

# ENERGY PRINCIPLE

## First Law of Thermodynamics

For a given system

$$\Delta E = Q - W$$

$$\frac{dE}{dt} = \dot{Q} - \dot{W}$$

Where:


*Q = Heat transferred to the system (positive sign)*

*W = Work transferred out of the system (negative sign)*

**E = (Internal Energy, Kinetic Energy, Potential Energy)**

$$E = U + K.E + P.E$$

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$$\dot{Q} - \dot{W} = \frac{d}{dt} \int_{cv} (u + e_K + e_P) \rho dQ + \int_{cs} (u + e_K + e_P) \rho V \bullet dA$$


$$e_K = \frac{(1/2)mv^2}{m} = \frac{v^2}{2}$$

$$e_P = \frac{mgz}{m} = gz$$

Mass flow rate

$$\dot{Q} - \dot{W} = \frac{d}{dt} \int_{cv} \left(u + \frac{v^2}{2} + gz\right) \rho dQ + \int_{cs} \left(u + \frac{v^2}{2} + gz\right) \rho V \bullet dA$$

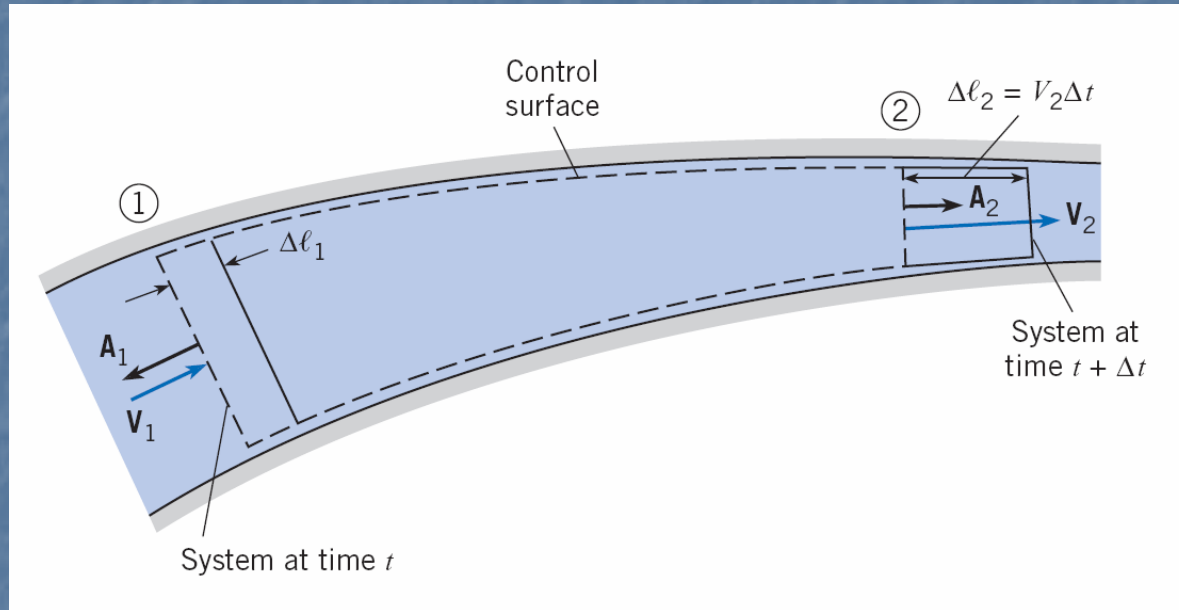
The Work  $\dot{W} = \dot{W}_f + \dot{W}_s$

$\dot{W}_s = \text{Shaft Work}$

$\dot{W}_f = \text{Flow Work}$

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## Flow Work



The flow of work done by the system at station (2) is given by

$$W_{f2} = F \times \Delta l_2 = (p_2 A_2) \times v_2 \Delta t$$

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$$\dot{W}_{f2} = (p_2 A_2) \times v_2 = p_2 v \cdot A$$

The flow of work by the system at station (1) is given by

$$W_{f1} = F \times \Delta l_1 = (p_1 A_1) \times V_1 \Delta t$$

$$\dot{W}_{f1} = (p_1 A_1) \times V_1 = p_1 V \cdot A$$

In general form, the work done by the system for a constant velocity

$$\dot{W}_f = \sum_{CS} p V \cdot A$$

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In general form, the work done by the system for a variable velocity

$$\dot{W}_f = \int_{CS} p \mathbf{V} \cdot d\mathbf{A} = \int_{CS} \frac{p}{\rho} (\rho \mathbf{V} \cdot d\mathbf{A})$$

Shaft Work ( $\dot{W}_s$ )

Consider Eqn.

$$\dot{Q} - \dot{W} = \frac{d}{dt} \int_{CV} \left( u + \frac{v^2}{2} + gz \right) \rho dQ + \int_{CS} \left( u + \frac{v^2}{2} + gz \right) \rho \mathbf{V} \cdot d\mathbf{A}$$

$$\dot{Q} - \dot{W}_s - \dot{W}_f = \frac{d}{dt} \int_{CV} \left( u + \frac{v^2}{2} + gz \right) \rho dQ + \int_{CS} \left( u + \frac{v^2}{2} + gz \right) \rho \mathbf{V} \cdot d\mathbf{A}$$

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$$\dot{W}_f = \int_{CS} p \mathbf{V} \cdot d\mathbf{A} = \int_{CS} \frac{p}{\rho} (\rho \mathbf{V} \cdot d\mathbf{A})$$

$$\dot{Q} - \dot{W}_s - \int_{CS} \frac{p}{\rho} (\rho \mathbf{V} \cdot d\mathbf{A}) = \frac{d}{dt}_{CV} \int (u + \frac{v^2}{2} + gz) \rho dQ + \int_{CS} (u + \frac{v^2}{2} + gz) \rho \mathbf{V} \cdot d\mathbf{A}$$

$$\dot{Q} - \dot{W}_s = \frac{d}{dt}_{CV} \int (u + \frac{v^2}{2} + gz) \rho dQ + \int_{CS} (u + \frac{v^2}{2} + gz) \rho \mathbf{V} \cdot d\mathbf{A} + \int_{CS} \frac{p}{\rho} (\rho \mathbf{V} \cdot d\mathbf{A})$$

$$\dot{Q} - \dot{W}_s = \frac{d}{dt}_{CV} \int (u + \frac{v^2}{2} + gz) \rho dQ + \int_{CS} (u + \frac{p}{\rho} + \frac{v^2}{2} + gz) \rho \mathbf{V} \cdot d\mathbf{A}$$

$$\text{The term enthalpy} = h = \left( u + \frac{p}{\rho} \right)$$

$$\dot{Q} - \dot{W}_s = \frac{d}{dt}_{CV} \int (u + \frac{v^2}{2} + gz) \rho dQ + \int_{CS} (h + \frac{v^2}{2} + gz) \rho \mathbf{V} \cdot d\mathbf{A}$$

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## Steady Flow Energy Equation

For steady flow, the flow accumulation equal zero and if the velocity distribution is constant, then

the Eqn.  $\dot{Q} - \dot{W}_s = \frac{d}{dt} \int_{CV} (u + \frac{v^2}{2} + gz) \rho dQ + \int_{CS} (h + \frac{v^2}{2} + gz) \rho \mathbf{V} \cdot d\mathbf{A}$  becomes

$$\dot{Q} - \dot{W}_s = \sum_{CS} \dot{m}_{out} \left( \frac{V^2}{2} + gz + h \right)_{out} - \sum_{CS} \dot{m}_{in} \left( \frac{V^2}{2} + gz + h \right)_{in}$$

**END OF LECTURE**  
**(1)**